PROBLEM 1

Calculate the flux of the vector field:

$$grad\left(\frac{1}{\sqrt{(x-3)^{2}+(y+1)^{2}+z^{2}}}+xy^{3}\right)$$

On a sphere with radius 3 and centre in the point (2,1,1)

PROBLEM 2

A quadrupole in the origin produce the vector field:

$$\frac{3\cos^2\theta-1}{r^4}\hat{e}_r + \frac{\sin 2\theta}{r^4}\hat{e}_\theta$$

Use the Gauss' theorem to calculate the flux on the cylinder:

$$\begin{cases} x^2 + y^2 \le 9\\ -1 \le z \le 2 \end{cases}$$

PROBLEM 3

Calculate the following line integral:

$$\oint_{L} \frac{2}{\rho} \hat{e}_{\varphi} \cdot d\overline{r}$$

where the path L is the one shown in the figure.

